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Integrated optics dissipative soliton mode-locked laser on glass.

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ABSTRACT

Mode-lock lasers have been studied a lot in the past years for producing pulses as short as possible. These devices have mostly been realized in bulk optics and they are consequently cumbersome and sensitive to vibrations. There are only a few studies on integrated optics mode-lock lasers, though this technology is very promising because of its stability, compactness and the possibility to integrate several functions on a single chip. In this paper, we present an ion-exchange passively mode-locked laser in dissipative soliton operation. One of the key characteristics of this structure is its mechanical stability. Indeed, no bulk optics is needed because the saturable absorber is hybridized on the top of the waveguide in order to interact with the evanescent part of the guided mode. Indeed, the device that has been obtained is composed of an ion-exchanged single mode waveguide realized in a Neodymium doped phosphate glass. The laser feedback is produced by a Fabry-Perot cavity realized with two multilayers dielectric mirrors stuck on the waveguides facets. We implemented a bis(4-dimethylaminodithiobenzil)nickel (BDN) dye included in a cellulose acetate thick film, which presents a saturable absorber behaviour around 1.06 μm . With this structure, pulses with repetition rates of 3.3 GHz and a single mode output have been measured. Moreover, the use of an autocorrelation set-up allowed us measuring picosecond pulse durations.

Keywords: Integrated optics, ion-exchange, mode-locked laser, dissipative soliton

1. INTRODUCTION

Ion-exchange on glass, which provides low propagation losses waveguides with a coupling with optical fiber^[1] has been a major technology in the field of integrated optics for more than thirty years. It allowed producing numerous passive devices with applications ranging from optical communication duplexers^{[2],[3]} to astronomy^{[4],[5]}. Moreover, the use of rare-earth doped glass has allowed realizing active devices like amplifiers^{[6],[7]}, continuous wave lasers^{[8],[9]} and Q-switched lasers^[10]. Nonetheless, there are only few studies on glass integrated optics mode-locked lasers, though this technology is very promising because of its stability, compactness and the possibility to integrate several functions on a single chip. In the last decades, mode-locked lasers for ultra short pulse generation have been studied over a wide range of configurations. This the first analytical theory of passive mode-locking was developed in 1975 by Haus and al.^[11]. The first mode-locked laser on glass integrated optics, which was working in the soliton operation has been realized by Pudo et Al.^[12]. But more recently, dissipative soliton operation has been investigated on optics fiber^{[13],[14]}. Unlike classical soliton lasers which operate with opposite signs for Self-Phase Modulation (SPM) and Group Velocity Dispersion (GVD), dissipative soliton lasers operate in normal dispersion regime. The pulse shaping is then determined by the interplay of SPM, GVD, which both shrink the pulse and the filtering effect linked to the finite gain bandwidth of the amplifying medium, which limits the pulse shrinking. Dissipative soliton lasers generate highly chirped pulses, which may be compressed outside the laser cavity. An interesting characteristic of these lasers is their capacity to produce a coherent multi-wavelength output pulse^[15]. Such a feature is expected to have versatile applications including photonics device characterization and terahertz generation. This kind of mode-locked laser operation has only been realized with optical fiber. In this paper, we present a fully integrated

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passively mode locked laser made by ion exchange which supports dissipative soliton operation at a wavelength of 1053 nm. The second part of this article is devoted to presenting the device, the realization process with the waveguide design as well of passive characteristics of the device, whereas section 3 deals with the laser finalization and pulses characteristics. Then, section 4 presents the theory on dissipative soliton operation for mode-locked laser.

2. DECIVE STRUCTURE AND PRINCIPLE OF OPERATION

The structure of the hybrid mode-locked laser is presented on figure 1, it is composed of three main parts.

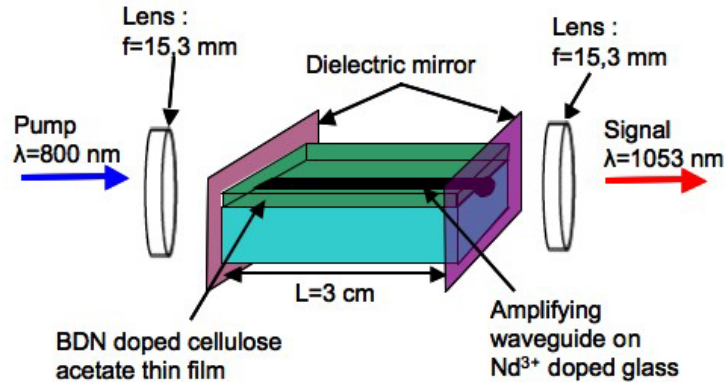


Figure 1: Schematic view of the hybrid mode-locked laser structure

First, it consists of a single mode amplifying waveguide realized by Ag^+/Na^+ ion-exchange on a $1.5 \times 10^{26} \text{m}^{-3}$ neodymium doped phosphate glass (IOG1 from Shott). The amplifying waveguide is pump with a 180 mW Sapphire Titan laser at $\lambda_p = 800 \text{ nm}$, which is focused into the waveguide. And acts as an amplifier at $\lambda_s = 1053 \text{ nm}$, which is due to the Nd^{3+} transitions in phosphate glass. Then, a bis(4-dimethylaminodithiobenzil)nickel (BDN) dye doped Cellulose Acetate (CA) thin film is deposited on the waveguide surface. It acts as a saturable absorber. The interaction between the laser mode and the saturable absorber is made through the evanescence part of the guided mode at signal wavelength as presented on figure 2. Indeed, the CA refractive index is 1,48, which is lower than the glass one of 1,51. This interaction can thus be characterized by the overlap integral between the guided mode and the superstrate. Finally, two dielectric mirrors are stuck on each facet to close the laser cavity. One present a 99.99% reflectivity at the signal wavelength for the input facet and one of 80% reflectivity at the signal wavelength for the output one. They both have reflectivity lower than 4% at pump wavelength

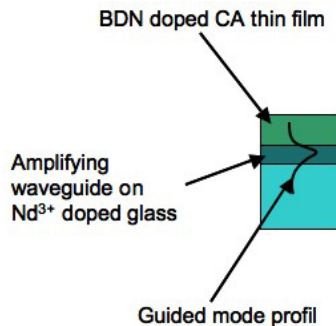


Figure 2: Transverse view of the structure

3. WAVEGUIDE

3.1 AMPLIFYING WAVEGUIDE REALIZATION PROCESS FLOW

The amplifying waveguide has been realized on a phosphate glass (IOG-1 from Schott) doped with $1.5 \times 10^{26} \text{ m}^{-3}$ Nd^{3+} ions with the process flow depicted on figure 3. First, the glass wafer has been degassed during 2 days in a vacuum furnace at 150°C in order to remove all the water absorbed on the glass surface. Secondly, a 30 nm thick silicon layer has been deposited on the wafer surface by RF sputtering. This layer will act as a mask during the ion-exchange step. Then, after lithography, a 3 cm long aperture has been etched in the silicon layer using a reactive ion etching with a SF_6 gas. The next step consists in the ion-exchange that we will design and simulate in during the next part. Finally, the silicon mask is removed with the same reactive ion etching process than in step 4 and the waveguide facets are cut and polished in order to have low coupling losses.

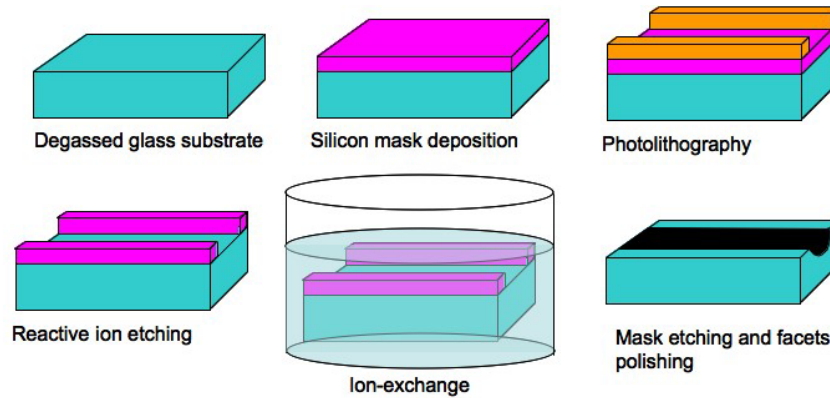


Figure 3: Process flow for amplifying waveguide realization

3.2 DESIGN OF THE AMPLIFYING WAVEGUIDE

In order to have a good control on the guided wave confinement and the on the interaction between the evanescent wave and the saturable absorber, the ion-exchange parameters should be design in order to obtain a single mode waveguide at pump and signal wavelength. Therefore, a model of the ion-exchange on phosphate glass is a necessary step before realizing the device.

3.2.1 ION-EXCHANGE MODELING FOR WAVEGUIDE REALIZATION

The refractive index variation, which allows the light confinement, is obtained by locally replacing some Na^+ ions of the glass substrate by Ag^+ , K^+ or Tl^+ ions. This doping is made thanks to a diffusion process that can be purely thermal or electrically assisted^[1]. Combining Fick-Fourrier's diffusion laws with the electro-neutrality one, allows deriving a relation linking the doping ion relative concentration, $c(x,y)$, to the ion-exchange parameters^[1]:

$$\frac{\partial c}{\partial t} = \frac{D_{dop}}{1-\alpha c} \left[\nabla^2 c + \frac{\alpha(\nabla c)^2}{1-\alpha c} - \frac{e}{k_B T H} \vec{\nabla} c \cdot \vec{E}_{ext} \right] \quad (1)$$

Where D_{dop} is the diffusion coefficient of the doping ions, $\alpha = 1 - D_{dop}/D_{Na}$ is the Stewart coefficient taking into account D_{Na} the diffusion coefficient of sodium, H is the Haven coefficient and \vec{E}_{ext} is the applied electric field. Although D_{dop} and D_{Na} are considered to be constant in simple models, in our case the mixed alkali effect can be taken into account following the approach proposed by Lupescu *et al*^[16].

For given exchange time, diffusion aperture width, applied electric field and surface concentration, the problem (1) is solved numerically using a finite difference algorithm with a Lax-Wendroff scheme^[17]. Once the doping ion concentration distribution has been computed, the resulting refractive index distribution is obtained through the simple proportionality relation derived from the model of Huggins *et al*^[18]:

$$n(x,y) = n_{sub} + \Delta n_{max} c(x,y) \quad (2)$$

where n_{sub} is the refractive index of the glass before the ion-exchange and Δn_{max} is the maximum refractive index variation obtained when $c(x,y)=1$.

This refractive index distribution can then be used as an input for a Scalar mode solver (3D Mode Solver by Optiwave Inc.) to determine the number of guided modes supported by the waveguide and their respective characteristics.

In our case, D_{dop} , which is the diffusion coefficient of silver ions, D_{Na} as well as the mixed alkali parameters have been determined using the m-lines method for different ion-exchanges concentrations.

3.2.2 ION-EXCHANGE PARAMETERS DETERMINATION

The amplifying waveguide is made of two ion-exchanges. Both are purely thermals and don't use any electric field. The first one is a Na^+/Ag^+ exchange, which is useful for setting the modicity of the waveguide and the second one is considered as a thermal burying in order to decrease the surface interaction and consequently the propagation losses that are due to surface roughness. The parameters for the first ion-exchange have been set in order to obtain a single mode waveguide at λ_p and λ_s : a duration of 4 min in a 20% silver nitrate / 80% sodium nitrate molten salt bath at 320°C and a diffusion aperture of 2 μ m. The glass substrate is the Nd^{3+} doped IOG1 phosphate glass from Shott. The second step consist in a 1 minute in a 100% sodium nitrate molten salt bath at 290°C ion-exchange, which is keep quick enough to not modify the wave confinement but finely tune the waveguide burying depth for low surface interaction. Indeed, a 5% interaction between the guided wave and the superstrate has been computed after simulation, which is still present and weak as desire.

The simulated mode field maps has been fitted by gaussians along the horizontal and vertical axes, leading to 1/e diameters of $6.2 \pm 0.1 \mu$ m and 1/e radius of $1.6 \pm 0.1 \mu$ m for the upper part and $3 \pm 0.1 \mu$ m for the bottom part respectively for the signal wavelength as depicted on figure 4a and to 1/e diameters of $5 \pm 0.1 \mu$ m 1/e radius of $1.3 \pm 0.1 \mu$ m for the upper part and $2.1 \pm 0.1 \mu$ m for the bottom part respectively for the pump wavelength as depicted on figure 4b.

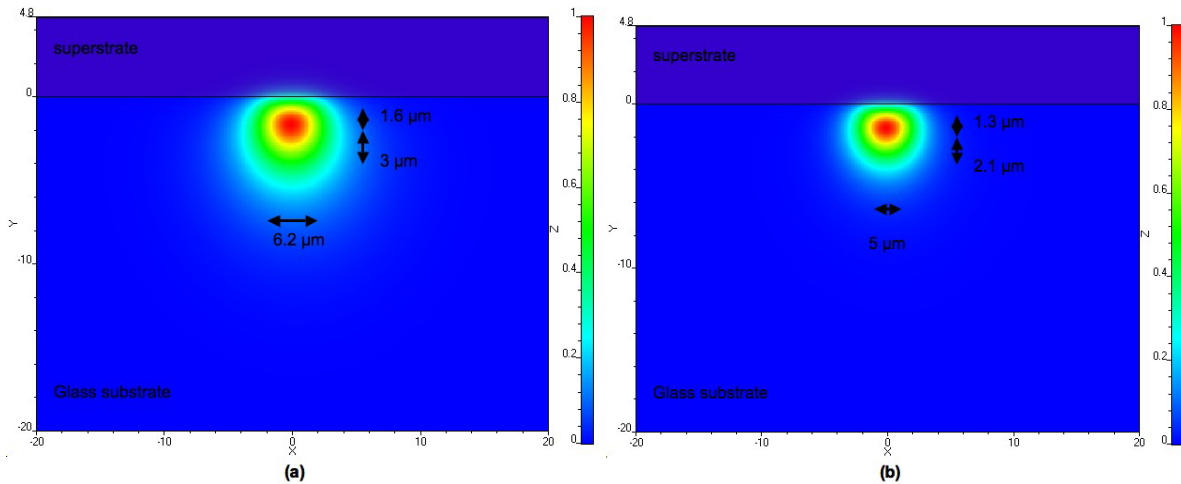


Figure 4: Field maps of the fundamental mode at $\lambda_s = 1053$ nm (a) and at $\lambda_p = 800$ nm (b).

3.3 PASSIVE CHARACTERISTICS OF THE DEVICE

The mode profiles of the waveguide has been measured at $\lambda_s = 1054$ nm and at $\lambda_p = 800$ nm by injecting light with a single mode optical fiber and imaging the waveguide output field through a microscope objective on a Silicon CCD camera as it is presented on figure 5. The waveguides are single mode at both wavelengths. The mode intensity map has been fitted by gaussians along the horizontal and vertical axes, leading to $1/e^2$ diameters of $7.6 \pm 0.7 \mu$ m and to a $1/e^2$ radius of $2.2 \pm 0.4 \mu$ m for the upper part and $2.8 \pm 0.4 \mu$ m for the bottom part

respectively at λ_s and to a $1/e^2$ diameters of $5.8 \pm 0.7 \mu\text{m}$ and to a $1/e^2$ radius of $2.1 \pm 0.4 \mu\text{m}$ for the upper part and $2.7 \pm 0.4 \mu\text{m}$ for the bottom part respectively at λ_p . We can notice that the mode fields diameters are close to the theoretical computation, which validate our model.

Replacing the CCD camera by a calibrated photo-detector, propagation losses of $0.3 \pm 0.1 \text{ dB.cm}^{-1}$ have been measured with and without an undoped CA cladding, which shows the good optical quality of the CA layer. One of those waveguides was used for all subsequent measurement and will be referred to as wg1. We also characterized a 0.7 dB.cm^{-1} waveguide, which will be referred as wg2.

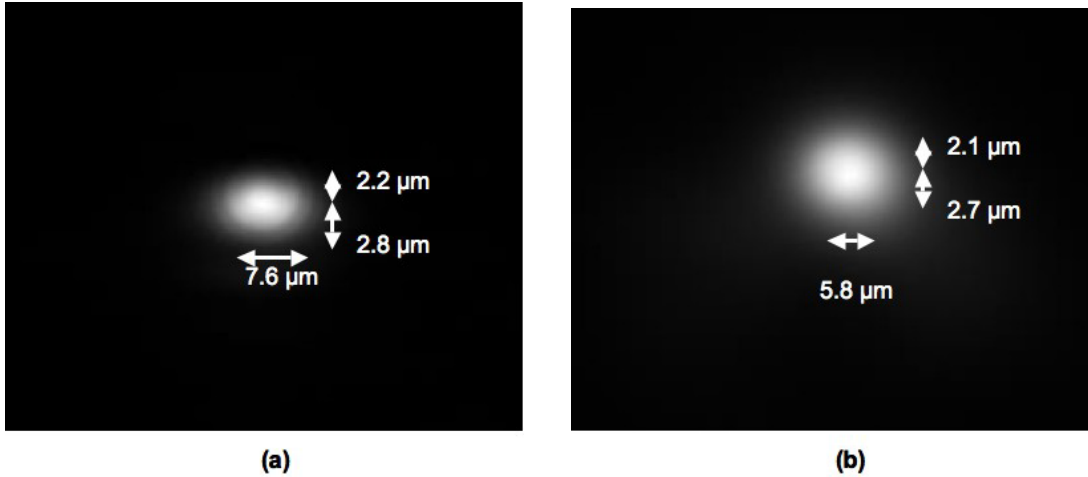


Figure 5: Measured intensity mode profiles at $\lambda_s = 1054 \text{ nm}$ (a) and at $\lambda_p = 800 \text{ nm}$ (b)

4. MODE-LOCKED LASER FINALIZATION AND CHARACTERIZATION

4.1.1 PROCESS FLOW

After realizing the amplifying waveguide, the saturable absorber is deposited on the substrate as it is depicted on figure 6a. First, a mixture of BDN and CA in an acetone solution is prepared in order to have a concentration of 1×10^{18} molecules of BDN per m^3 into the CA layer after polymerization. Secondly, the layer is deposited to be $100 \mu\text{m}$ thick, which is considered as infinite since only the evanescent wave is in interaction with it. Finally, the layer is dried in a furnace at 150°C under vacuum until complete polymerization. Finally, a 99.99% reflectivity dielectric mirror is stuck on the input facet and another one with a 80% reflectivity is stuck on the output facet as shown on figure 6b.

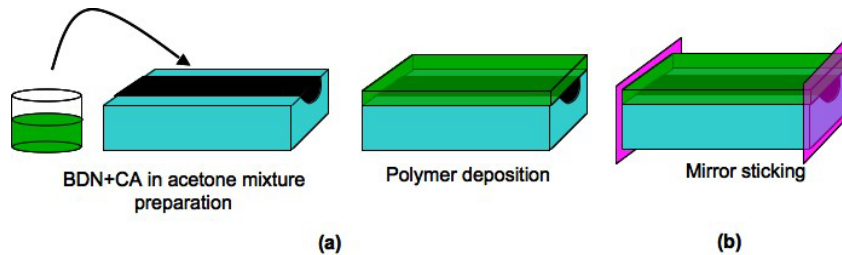


Figure 6: Saturable absorber preparation and deposition (a) and mirror sticking (b)

4.2 REPETITION RATE CHARACTERIZATION

Then, the device, which has been realized, has been characterized with a fast photodiode and an oscilloscope in order to verify the continuous mode-locking operation as depicted of figure 7.

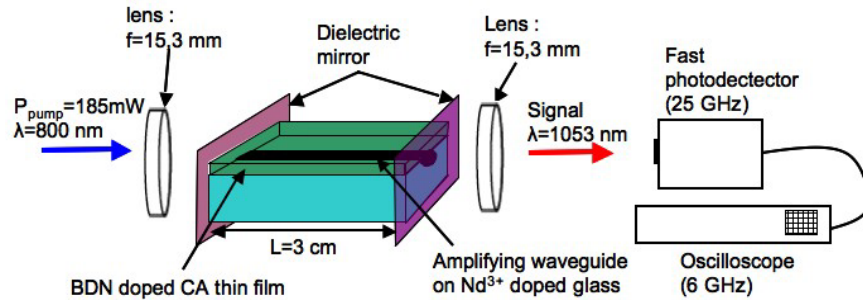


Figure 7: Schematic view of the characterization bench for repetition rate measurement.

For this characterization, the laser was pumped with a Sapphire-Titan laser that has been injected into the amplifying waveguide. The injected power has been previously measured at 185 ± 5 mW at $\lambda_p = 800$ nm. Then the output signal at $\lambda_s = 1053$ nm has been focalized on a 25 GHz photodiode linked to a 6 GHz oscilloscope. As we can see on figure 8, this method is useful for repetition rate characterization, which is in our case equal to 300 ps. This repetition rate corresponds to the photon round-trip time in the 3 cm laser cavity in the glass medium.

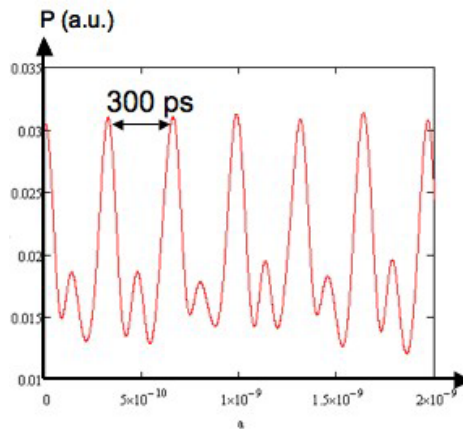


Figure 8: Oscilloscope trace of the output pulse train.

Now, there is still to determine the output pulse width because this method was not quick enough. Actually, the only way to determine the pulse width is the autocorrelation method.

4.3 PULSE WIDTH AND SPECTRUM CHARACTERIZATION

First, the wg2 waveguide, which was presented 0.7 dB/cm losses, has been characterized. It was emitting 10 ± 0.5 mW average power when pumped with 185 mW injected pump power. For characterizing the pulse shape, the fast photodiode of the bench on figure 8 has been replaced by an autocorrelator, which consists of Michelson interferometer and a CCD camera to visualize the visibility of the fringes that depends of the superposition of the pulses at the output of the Michelson interferometer. As depicted on figure 9a, the pulse temporal FWHM width of the autocorrelation trace has been measured to 2 ± 0.2 ps, which corresponds to a computed width of 1.3 ± 0.2 ps assuming a sech^2 -shape^[11]. We can underline than the corresponding spectrum of these pulses, which is depicted on figure 9b, consists of one 3 nm wide gate-shaped peak located around a wavelength of 1053 nm. This spectrum has a typical shape of single wavelength emission of a dissipative soliton operation mode-locked laser as described by Zhang et al.^[15].

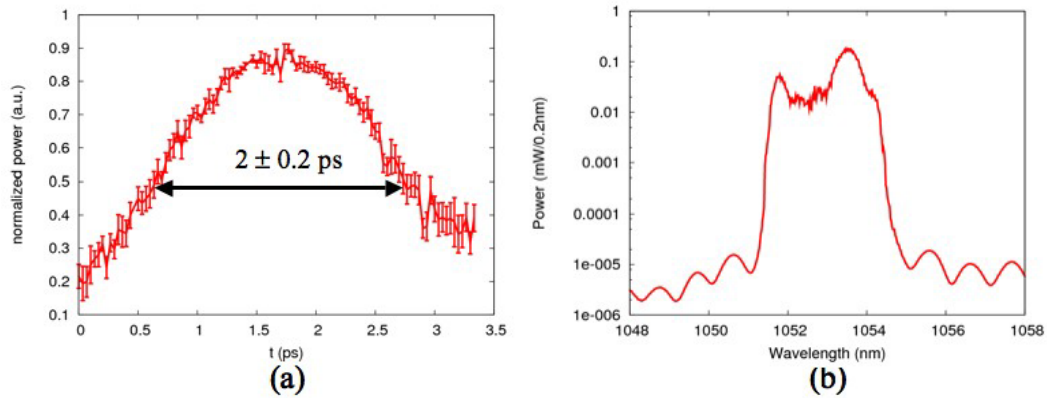


Figure 9: Autocorrelation trace (a) and spectrum (b) of a single wavelength pulse (laser wg2).

Then, for the laser based on waveguide wg1, double-frequency dissipative soliton pulses have been observed. Indeed, the spectrum presented on figure 10b clearly contains two gate-shaped peaks located around a wavelength of 1053nm. From the autocorrelation trace presented on figure 10a, a temporal FWHM width has been measured to 3.5 ± 0.2 ps, which corresponds to a computed width of 2.3 ± 0.2 ps. For this device, the average output power 30 ± 0.5 mW when pump with a 185 mW injected pump power. The interference pattern in the autocorrelation function confirms the coherent dual-wavelength nature of the pulse. It can be noticed that the 0.4 ps period of the autocorrelation pattern (fig 10a) corresponds to the 2.2 nm or 600 GHz spacing between the two peaks of the spectrum (fig. 10b).

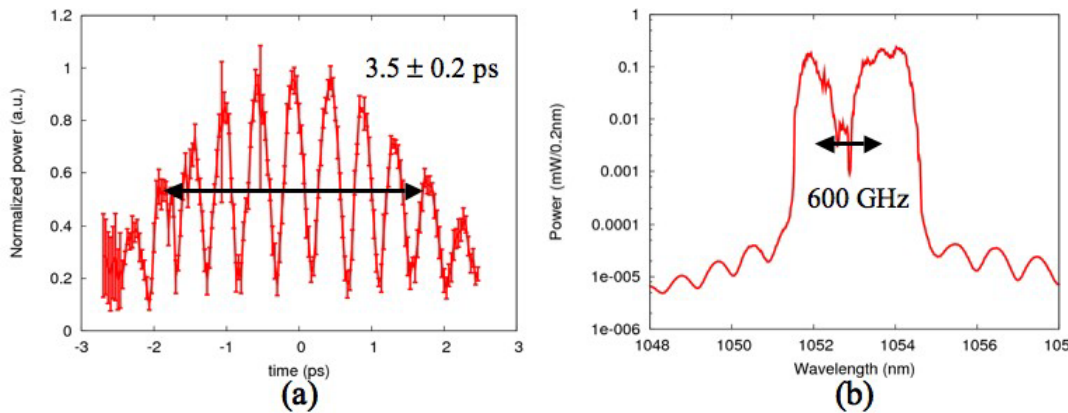


Figure 10: Autocorrelation (a) and spectrum (b) of a double wavelength pulse (laser wg1).

5. DISCUSSION

We can underline the fact that BDN concentration is very low in this device. Indeed, saturable losses are computed to be 0.01 dB/cm, which is very weak compared to the small signal gain of ___ dB/cm. We consequently can assume that the pulse formation is not only due to the saturable absorber, but other phenomena have to be taken into account for the modeling the pulse shaping in this kind of mode-locked laser. Indeed, if we model passive mode-locking following this equation (3), the saturable absorber losses parameter is very weak compared to the gain and constant losses ones so that it can be neglected in this model.

$$\frac{\partial A(z,t)}{\partial z} = (g(z,t) - q(z,t) - l) \cdot A(z,t) \quad (3)$$

Where $A(z,t)$ is the complex pulse envelop, which depend on the position in the laser cavity z following the pulse envelop at time t , $g(z,t)$ is the gain in position z at time t , $q(z,t)$ is the saturable absorption in position z at time t and l is the constant loss parameter, which represents the propagation losses and the mirror losses.

Indeed, because of the wave confinement characteristic of the laser in a glass medium, two other phenomena have to be taken into account. First, the GVD parameter, which depend of the confinement of the guided mode as well as the waveguide media, is described in equation (4):

$$\frac{\partial A(z,t)}{\partial z} = -i \cdot D_2 \cdot \frac{\partial^2 A(z,t)}{\partial t^2} \quad (4)$$

Where D_2 is the chromatic dispersion parameter of the waveguide.

In our case, the mode profile being similar than in optical fiber and the medium being phosphate glass, we can consider than we are in all normal dispersion operation with the parameter $D_2 > 0$ in equation (4) like in phosphate optical fiber. Moreover, in mode-lock operation regime, the power density is as high as the non-linear refractive index of the phosphate glass is no more negligible. Indeed, the refractive index of the glass n is:

$$n = n_0 + I \cdot n_2 \quad (5)$$

Where n_0 is the constant refractive index of the medium ($n_0 = 1.52$ in our case), I is the intensity of the guided mode and n_2 is the non-linear refractive index of the medium ($n_2 = 3.2 \times 10^{-20} \text{ m}^2/\text{W}$ in phosphate glass^[19]).

This coefficient stimulate the effects of SPM in our waveguide in this form:

$$\frac{\partial A(z,t)}{\partial z} = i \cdot \gamma \cdot |A(z,t)|^2 \cdot A(z,t) \quad (6)$$

Where $\gamma = \frac{2\pi \cdot n_2 \cdot c}{n_0 \cdot \lambda_s \cdot A_{eff}}$ is the non-linear coefficient, which depends of the non-linear refractive index n_2 , of

the light velocity under vacuum c , of the signal wavelength λ_s , and of the effective area of the guided mode A_{eff} .

Considering all these parameters and knowing than we are in an all-normal GVD mode of operation, the two phase phenomena, which the SPM and the GVD, are of the same sign so that they are not compensating each other. Consequently, another parameter has to be taken into account. Indeed, we have to consider the spectral filtering of the gain bandwidth, which will stabilize the mode-locking operation. This spectral filter can be consider like a parabolic attenuation as it is implemented in the non-linear Schrödinger equation (7):

$$\frac{\partial A(z,t)}{\partial z} = (g(z,t) - q(z,t) - l) \cdot A(z,t) + i \cdot \left(\gamma \cdot |A(z,t)|^2 + D_g \cdot \frac{\partial^2}{\partial t^2} - D_2 \cdot \frac{\partial^2}{\partial t^2} \right) \cdot A(z,t) \quad (7)$$

Where D_g is the half-width of the medium gain bandwidth.

This working principle is so called dissipative soliton mode-locking operation. This kind of operation mode produced highly chirped^[13] pulses and it also can produce multi-wavelength pulses^[15]. Moreover, the dissipative soliton non-linear Schrödinger equation determines a hyperbolic secant pulse shape^[11], which could be useful to know pulse width determination after autocorrelation measurement.

6. PERSPECTIVES AND CONCLUSION

In this paper, we presented the complete design, theoretical behavior and characteristics of a dissipative soliton operation in a fully integrated mode-locked laser. First, ion-exchange based technology made us able to elaborate a design in order obtain low loss and single mode amplifying waveguides. Then a theoretical study of the working principle of dissipative soliton allow us to understand the phenomena that have to be taken into account for the design of our device, which could still be optimized for having more non-linear effects or a

negative dispersion for compensative soliton generation. Moreover, numerical simulation using the non-linear Schrödinger equation for pulse shape prediction is under development in order to optimize the waveguide design. Finally, primary results that shows the dissipative soliton operation in the previously fabricated device, have been obtained. First, using a cavity with average losses, single-wavelength pulses of 1.3 ps width have been observed. The dissipative soliton operation predicts highly chirped pulses. An experiment to compress them by dechirping with a negative dispersion waveguide or optical fiber is under progress. Secondly, using low-losses waveguides, double frequency pulses have been characterized. This kind of pulse could be interesting for THz generation. Indeed, the two frequencies of the pulses are coherent, have a high peak power and are spaced by 600 GHz, which is close to the terahertz frequency domain. Finally, a triple wavelength pulse has been observed for a very low loss waveguide, so we think that under higher pump power, high order multi-wavelength operation is possible. Such pulses may be interesting for WDM optical communication systems.

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